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laudu mont vita PHYSICS

(Honours Elective)

Paper: PHY-HE-6056

constraint equations. How (Classical Dynamics)

Full Marks: 80

Distance ow Time: Three hours

The figures in the margin indicate full marks for the questions.

of the respective place Answer any ten from the following: 10 - X5V1100 XX 5V8V100 X 808 COMW 11×10=10

- Mention the device in a vehicle, which uses damping to perform a useful task.
- (b) If \vec{E} and \vec{B} represent electric and magnetic fields respectively then what

physical quantity does greater probability of having

represent?

Die an ving 208 Contd.

(c) Draw a diagram to indicate the location of the quantity l in the equation

$$\frac{1}{r} = \frac{1}{l} \left[1 + \varepsilon \cos(\theta - \theta_0) \right]$$

where the quantities carry their usual meanings.

- (d) In a system there are 1000 particles and 100 constraint equations. How many generalized co-ordinates will be needed to describe the system?
- (e) A liquid is coming out of two separate capillary tubes A and B of radii in the ratio r_A : $r_B = 2:3$. What is the ratio v_A : v_B of the speeds of the liquid coming out of the respective tubes?
- (f) On which side, concave or convex of a streamline the lateral pressure of the fluid is greater?
- (g) A fluid is flowing through two different tubes A and B having Reynold's numbers $R_A = 10,000$ and $R_B = 40,000$. In which tube the fluid motion has the greater probability of having a streamline flow?

- (h) Mention an experimentally observed phenomenon which confirms time dilation.
- (i) If L and H are respectively the Lagrangian and the Hamiltonian of a system then write the dimension of the quantity $=\frac{H}{L}$.
- (j) What are world points in Minkowski space?
- (k) If $\frac{\partial^2 y}{\partial x^2} = \left(\frac{A}{B}\right) \frac{\partial^2 y}{\partial t^2}$ represents a progressive wave, where A = 100 and B = 400 in SI units then find the speed of the wave.
- An experiment is performed on the earth and the inertial mass of a body is found to be 10 kg. The body is taken to the Moon. What will be the gravitational mass of the body on the Moon?
- (m) Mention a phenomenon in which energy is converted into mass in accordance with $E = mc^2$.
- (n) Mention a conclusion which can be drawn for a particle with total energy E and linear momentum p for which

$$E^2 - p^2c^2 < 0$$

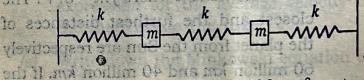
- (o) What condition the Lagrangian L of a system has to satisfy for the total energy of the system to be conserved? a) if a and H are respectively the
- 2. Answer any five of the following: 2×5=10
 - (a) Draw the curve $x^2 m^2 = -1$ in the Minkowski space in the proper quadrant(s), where x stands for space co-ordinates and m = ct stands for time co-ordinate.
 - (b) A particle of mass 2 µg and charge 2 C moving with a velocity $\vec{v} = \hat{k}10 \text{ ms}^{-1}$ enters a region in which both an electric field $\vec{E} = \hat{k}100 \text{ Vm}^{-1}$ and $\vec{B} = \hat{k}0.1 \text{ T}$ then find the kinetic energy gained by the particle when it undergoes a displacement of $\vec{l} = \hat{k} 2m$.
 - (c) A particle is moving in a curved path under the action of a central force. Its position co-ordinates at an instant t is $P(r,\theta)$. If the semi-latus rectum of the conic in which the particle moves, is equal to r then determine the shape of the orbit. E2 - p care

(d) The potential energy of a particle of mass 100 g capable of moving in the xdirection is given by

$$V = \alpha x^2 - \beta x$$

If the particle is at rest then at what position will it be in equilibrium? Here α and β are two positive constants.

- Is it possible to construct a simple pendulum in the laboratory? Justify your answer with reasons.
- Two identical particles, each of mass m are attached to three identical springs, each of stiffness constant k as shown in the figure. When one of the particles 05-4x2 is slightly displaced, the systems undergoes simple harmonic oscillations. privom What are the circular frequencies of i sixs to the normal modes of vibration of the SIT . System ?

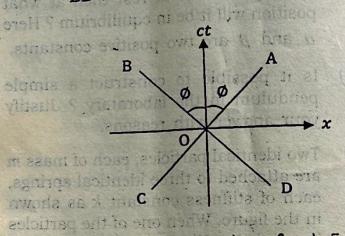


(g) A glass plate of area 100 cm² rests on a layer of oil of thickness 2 mm having co-efficient of viscosity 100 poise. Find the horizontal force needed to push the plate at a constant speed of 2 cm s-1.

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(h) What should be the maximum value of ϕ in the adjoining figure if a particle travelling at a speed v < c and v = c are represented by the world lines AC and BD?



- 3.79 Answer the following: (any four) 5×4=20
- (a) A planet of mass 2×10^{24} kg is moving in an elliptical orbit with major axis j and minor axis k where j:k=5:4. The closest and the furthest distances of the planet from the Sun are respectively 60 million km and 40 million km. If the time period of revolution of the planet around the Sun is 3.14×10^7 s then find the angular momentum of the planet around the Sun.

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(b) Write the definition of conservative force. Apart from gravitational force which other force is conservative in nature? Show that for a force \vec{F} to be conservative the following condition has to be satisfied:

$$\vec{\nabla} \times \vec{F} = \vec{0}$$

where $\vec{0}$ is a null vector.

- (c) A particle of mass m is moving along a circle of radius R under the action of a conservative force $\vec{F} = -m\omega^2 x \hat{i} m\omega^2 y \hat{j}.$ Find the potential energy of the particle.
- (d) What is called the critical velocity of a fluid in a tube? If v_o be the speed of a viscous fluid in streamline motion along the axis of a capillary tube of radius a and length l then find the expression for the average velocity of the fluid inside the tube.
- (e) Write down the Minkowski equation of motion in terms of the four force \vec{F}^{μ} for a particle of rest mass m_0 . Show that for the particle velocity v << c, where c is the speed of light in vacuum, the equation reduces to Newton's second law.

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- (g) Use the velocity four vector to derive the velocity addition theorem in special theory of relativity.
- (h) A viscous fluid of density 800 $kg m^{-3}$ and co-efficient of viscosity 100 poise is in streamline motion inside a tube of length 50 cm and radius R = 5 mm. The speed of the fluid varies with distance rmm from the axis of the tube

as $4\left(1-\frac{r}{5mm}\right)mms^{-1}$. Find the kinetic energy of the fluid within the tube.

4. Answer the following: (any four)
10×4=40

(a) What are generalized co-ordinates? Mention any two characteristics of generalized co-ordinates. How the number of generalized co-ordinates needed for a system of particles related to the number of degrees of freedom of the system? State the principle of virtual work and derive d'Alembert's equation from the principle of virtual work.

1+2+1+6=10

Deduce Euler-Lagrange's equation from d'Alembert's principle.

(b) What is generalized force? Deduce an expression for the m^{th} component of generalized force for a system consisting of n number of particles. A particle of mass m is moving in a three dimensional space under the action of a force $\vec{F} = \hat{i}F_x + \hat{j}F_y + \hat{k}F_z$ in free space. If a (x, y, z) be the co-ordinates specifying the location of the particle at an instant t then find the expression for the kinetic energy of the particle at that instant. Using the general form of Lagrange's equation arrive at the following equations

$$F_x = m\ddot{x}$$

$$F_y = m\ddot{y}$$

$$F_z = m\ddot{z}$$

$$1+3+3+3=10$$

(c) From the definition of the Hamilton of a system derive Hamilton's equations of motion. Hence, show that the Hamiltonian of the system is a constant of motion if the Lagrangian of the system is not an explicit function of time. With the help of a few mathematical steps explain the physical significance of the Hamiltonian of a system.

(d) Using Hamilton's canonical equation show that

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- the angular momentum of a particle moving in a central force field is conserved
- number of rarricles. A particle of (ii) the particle moves according to Kepler's first law in gravitation.

- space if a th we be the co-ordinates (e) In a system N identical particles are coupled by (N+1) identical springs of to an stiffness constant k each. If the system undergoes longitudinal oscillations then find the expression for the normal frequencies of vibration of the system. What is 'out of phase' oscillation? Show that when the system vibrates, it not generates a longitudinal wave. Find the expression for the speed of the 5+1+3+1=10 ingten wave. ... take and to ne not
 - (f) What is four vector? Using velocity, momentum and force four vectors derive the Einstein mass-energy Of the equivalence relation $E = mc^2$. 2+8=10

of motion if the Leerengian of the

- 10 (g) What is Doppler effect in light? How it edist is different from a similar phenomenon anoma in sound? What insight Doppler effect classic in light has given regarding the Universe ? Using four vectors find the expression for wavelength shift $\Delta\lambda$ of light emitted by a source in relative motion with the observer. A star emits light at the frequency 5×10¹⁷ Hz. If the star is receding away from the earth at a speed 3×103 km s-1 then find the percentage change in the frequency of the light due to Doppler effect. 1+1+1+5+2=10
- What is Minkowski's four dimensional (h) space? What is called world line in this space? Draw the world line of a ray of light and that of moving particle in a single diagram. Show that the space-time interval is invariant under Lorentz transformation. 1+1+2+6=10
 - A photon of energy hv_0 undergoes an elastic collision with a free electron of rest mass m_0 . Using the invariance of scalar product of two four vectors under Lorentz transformation find the expression for the Compton scattering wavelength shift of the photon.

(j) Deduce Poiseuille's equation for flow of a viscous liquid through a tube. Mention the simplified assumptions present in the deduction of the formula due to which the corrections are needed.

Three capillary tubes of equal length have internal diameters 2 mm, 4 mm and 6 mm are connected one after another. A viscous liquid flows through the system. If the pressure difference across the whole system is 2×10^5 Pa then find the pressure difference across the first tube.

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4+2+4=10