Total number of printed pages-8 DITLA BURGH MALLANDE 3 (Sem-5/CBCS) PHY HC 1 probability of readilytor Statude long lebies 2022 How I Bershi PHYSICS ob wold 4 randahav The number (Honours) ed electrostates 101 Paper : PHY-HC-5016 (Quantum Mechanics and Applications) Full Marks : 60 Time : Three hours The figures in the margin indicate full marks for the questions. 1. Answer any seven of the following :

(a) Write down the expression of wave function of matter wave associated with a free particle travelling along the x-axis having momentum p and energy E.

b) Is the function  $\psi = a \cos m \phi$  an eigenfunction of z-component of angular momentum operator ? Give reason.

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(c) Why  $\psi = ax^2$  is not an acceptable wave function in quantum mechanics?

- (d) Write down the condition of of orthogonality of wave function.
- (e) When does the quantum mechanical probability of oscillator become identical with the classical probability?
- (f) How do you represent dynamical variables in quantum mechanics ?
- (g) The number of permitted eigenvalues in a finite potential well is :
  - (i) two and an an an and an an and
  - (ii) zero
  - (iii) fixed for well of any height
  - (iv) variable, depending on the height of the well
- (h) What is the total number of energy level (or degeneracy) for the nth state of hydrogen atom ?
- (i) Why does the normal Zeeman effect occur only in atoms with even number of electrons ?
- (j) What is the need of an inhomogeneous magnetic field in Stern-Gerlach experiment ?
  - (k) The spin-orbit interaction has no effect on

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- (i) f-state
  - (ii)  $\delta$ -state
  - (iii) d-state(iv) p-state
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SWAWS

## (1) What is Bohr magneton ?

- 2. Answer any four of the following : 2×4=8
- (a) What are the conditions and limitations that the wave function must obey ?
- (b) Show that  $[\hat{x}^n, \hat{P}_x] = i\hbar nx^{n-1}$
- (c) The one-dimensional wave function is
- given by  $\psi(x) = \sqrt{a} e^{-ax}$ . Find the probability of finding the particle
  - between  $x = \frac{1}{a}$  and  $x = \frac{2}{a}$ .

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- (d) What is a Gaussian wave packet ? Express its wave function.
- (e) For a free particle, show that the group velocity of the wave packet is equal to the classical velocity of the particle.
- (f) What do you mean by Larmor precession ? What is Larmor frequency ?
  - (g) Determine the value of spin magnetic momentum of free electron.
  - (h) Determine the possible values of resultant angular momentum for two electrons having  $j_1 = \frac{3}{2}$  and  $j_2 = -\frac{5}{2}$ .

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excited state

(e) What is the significance of zero point energy ? Calculate the zero point DEHEXO energy for an oscillating mass of 1gm connected to a spring, which is rom tine stretched 1 cm by a force 0.1N. The gnioubo particle is constrained to move along off the the x-axis. 2+3=5

(f) Derive an expression for orbital magnetic moment due to electron rotating arround the nucleus of an atom. What is Bohr magneton ? 4+1=5

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What is Lande's g-factor ? Calculate E-1 (g) the Lande's g-factor for the  $3P_1$  state. SOFTBOIR: Use the result to predict the splitting of the energy level when the atom is placed in an external magnetic field of 0.1 Tesla.

(Given Bohr magneton =  $9.3 \times 10^{-24} Am^2$ ) by the 1+1+3=5 wave function  $\nu(x) \neq Ae^{ixi} \sin \alpha x$ 

(h) The atomic number of Beryllium is 4. Determine its 18-4+1

(i) electronic configuration in ground state. t (ii) given by

electronic configuration in first excited state. as nweni

spectroscopic terms in the ground (iii) .summa of .: state. Way nerected

> (iv) spectroscopic terms in the first excited state.

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Answer any three of the following : 3. 5×3=15

(a) In what respect does Schrödinger equation differ from classical wave bris equation ? Obtain the three-dimensional noisshin time independent Schrödinger equation from the time-dependent form. 1+4=5

(b) What do you understand by the wave function  $\psi$  of a moving particle ? Give BI GOLD its physical significance. What does selt the square of wave function signify ? alottisa 1+2+2=5

What is an operator ? Write the (c)expression for position operator, momentum operator and energy operator. What is Hamiltonian quois operator ? 1+3+1=5 ker is equal to

(d) Use the time independent Schrödinger equation to find V(x) and energy E for Svonoup which the wave function is

observed to  $\psi(x) = \left(\frac{x}{x_0}\right)^n e^{-x/x_0}$ in Determine the possible values of own not where n and  $x_0$  are constants. - Assume  $V(x) \rightarrow 0$ , as  $x \rightarrow \infty$ .

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## 4. Answer any three of the following : 10×3=30

for an oscillating mass of 1 mm (a) (i) What is the need for differential wave equation ? Starting from the wave equation and introducing energy and momentum of the particle, obtain expression for one dimensional Schrödinger time dependent wave equation for waves associated with a moving particle in a potential field V. rosoal-o abbral ei JanW 1+4=5

is Lande's g-factor for the SP, state. What is the physical significance and in (u) of  $\int |\psi|^2 dx = 1$ ?

A particle is represented by the wave function  $\psi(x) = Ae^{-|x|} \sin \alpha x$ Evaluate the normalization constant A,  $\alpha$  being a constant. 1+4=5the configuration in ground Calculate the normalization constant for a wave function (at t = 0) given by suration in first  $\psi(x) = ae^{-(a^2x^2)/2}e^{ikx}$  known as Gaussian wave packet. Determine. (ii) the probability density and

(iii) probability current density for 155115 this function.

the snomalous Zeeman effect

4+2+4=10

- (c) Write the radial equation of Hydrogen atom and solve it for obtaining its energy eigenvalues. 2+8=10
- Discuss classical and quantum (d)interpretations of square well potential of finite depth and determine allowed values of energy using graphical method. Also sketch the wave functions corresponding to three lowest energy levels.
- What are symmetric and anti-(e) (i) symmetric wave functions ?

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- State and explain Pauli's *(ii)* exclusion principle. How does a knowledge of symmetric and antisymmetric wave functions lead to this principle ? 5+3=8
- Describe and explain LS and JJ *(f)* couplings. Illustrate them with vector diagram. Give the selection rules for L. S and J. 2+2+4+2=10

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2+3+5

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Calculate

(b) (i)

 (g) Elucidate anomalous Zeeman effect using concept of 'spin' of electrons. Illustrate the anomalous Zeeman effect for Sodium D-lines. 6+4=10

(h) Write short notes on any two of the following : 5×2=10

(i) Stern-Gerlach experiment
(ii) Paschen-Back effect
(iii) Stark effect

fanctions corresponding to three

lowest etter gir levels

) What are symmetric and anuavecations wave functions ? 2

) State and explain Pauli's exclusion principle. How does a knowledge of symmetric and antisymmetric wave functions lead to this principle 2 = 0 0 5 588=8

) Describe , and explain LS and JJ couplings. Illustrate them with vector diagram, Give the selection rules for L, S and J.

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